### High-Fidelity Multidisciplinary Design Optimization for the Next Generation of Aircraft

#### Joaquim R. R. A. Martins http://mdolab.engin.umich.edu

Congress on Numerical Methods in Engineering • Lisbon, Portugal • July 1st, 2015

Numerical methods have been playing an increasing role in engineering analysis

Experiments

Numerical simulations







#### 40% fewer wind tunnel days

[Airbus A380 - RAe Hamburg & VDI January 2008]

Once numerical simulations are developed, they can be used for design optimization



Design optimization problem: minimizef(x)objectivewith respect toxdesign variablessubject to $c(x) \le 0$ constraints

Complex systems require the consideration of multiple disciplines, hence MDO was born

Aerodynamics Structures Stability & control Weights Loads Noise Materials Mission

JAL B787 climbing after takeoff from SAN • © J.R.R.A. Martins 2013

#### Research in the Multidisciplinary Design Optimization Laboratory is divided into two main thrusts

#### Fundamental MDO algorithms



## With 90,000 daily flights, improvements in aircraft performance has a huge impact



### Airplane fuel burn per seat has decreased by over 80% since the first jet





# The next generation of aircraft demands even more of the design process

- Highly-flexible high aspect ratio wings
- Unknown design space and interdisciplinary trade-offs
- High risk

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## Want to optimize both aerodynamic shape and structural sizing, with high-fidelity



### 3 major challenges



1. Computational costly to evaluate objective and constraints





3. Large numbers of design variables, design points and constraints High-Fidelity Multidisciplinary Design Optimization for the Next Generation of Aircraft

Choice of optimization algorithm
 Computing derivatives efficiently
 Aerodynamic shape optimization

Aerostructural design optimization

Summary and ongoing work

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### Gradient-based optimization is the only hope for large numbers of design variables



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Gradient-based optimization requires gradient of objective and Jacobian of constraints

$$egin{aligned} & \min_{x \in \mathbb{R}^n} & f(x,y(x)) \ & ext{s.t.} & h(x,y(x)) = 0 \ & g(x,y(x)) \leq 0 \end{aligned}$$

*x*: design variables

y: state variables, determined implicitly by solving R(x, y(x)) = 0

Need df/dx (and also dh/dx, dg/dx).

### Methods for computing derivatives

Monolithic Black boxes input and outputs	Finite-differences	$\frac{\mathrm{d}f}{\mathrm{d}x_j} = \frac{f(x_j + h) - f(x)}{h} + \mathcal{O}(h)$		
	Complex-step	$\frac{\mathrm{d}f}{\mathrm{d}x_j} = \frac{\mathrm{Im}\left[f(x_j + ih)\right]}{h} + \mathcal{O}(h^2)$		
Analytic Governing eqns state variables	Direct Adjoint	$\frac{\mathrm{d}f}{\mathrm{d}x} = \frac{\partial f}{\partial x} - \frac{\partial f}{\partial y} \begin{bmatrix} \partial R \\ \partial y \end{bmatrix}^{-1} \frac{\partial R}{\partial x}$		
Algorithmic differentiation <i>Lines of code</i> <i>code variables</i>	Forward $\begin{bmatrix} 1 & 0 & \cdots & 0 \\ -\frac{\partial T_2}{\partial t_1} & 1 & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ -\frac{\partial T_n}{\partial t_1} & \cdots & -\frac{\partial T_n}{\partial t_{n-1}} \end{bmatrix}$	$\begin{bmatrix} 1 & 0 & \dots & 0 \\ \frac{\mathrm{d}t_2}{\mathrm{d}t_1} & 1 & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0 \\ \frac{\mathrm{d}t_n}{\mathrm{d}t_1} & \dots & \frac{\mathrm{d}t_n}{\mathrm{d}t_{n-1}} \end{bmatrix} = I = \begin{bmatrix} 1 - \frac{\partial T_2}{\partial t_1} \dots & -\frac{\partial T_n}{\partial t_1} \\ 0 & 1 & \ddots & \vdots \\ \vdots & \ddots & \ddots & -\frac{\partial T_n}{\partial t_{n-1}} \\ 0 & \dots & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \frac{\mathrm{d}t_2}{\mathrm{d}t_1} \dots & \frac{\mathrm{d}t_n}{\mathrm{d}t_1} \\ 0 & 1 & \ddots & \vdots \\ \vdots & \ddots & 1 & \frac{\mathrm{d}t_n}{\mathrm{d}t_{n-1}} \\ 0 & \dots & 0 & 1 \end{bmatrix}$		

[Martins and Hwang, AIAA Journal, 2013] [Martins et al., ACM TOMS, 2003]

### Analytic methods evaluate derivatives by linearizing the governing equations

Need df/dx (and also dh/dx, dg/dx), f(x, y(x))

$$\frac{\mathrm{d}f}{\mathrm{d}x} = \frac{\partial f}{\partial x} + \frac{\partial f}{\partial y}\frac{\mathrm{d}y}{\mathrm{d}x}$$

Derivative of the governing equations: R(x, y(x)) = 0

$$\frac{\mathrm{d}R}{\mathrm{d}x} = \frac{\partial R}{\partial x} + \frac{\partial R}{\partial y}\frac{\mathrm{d}y}{\mathrm{d}x} = 0 \quad \Rightarrow \quad \frac{\partial R}{\partial y}\frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{\partial R}{\partial x}$$

Substitute result into the derivative equation

$$\frac{\mathrm{d}f}{\mathrm{d}x} = \frac{\partial f}{\partial x} - \frac{\partial f}{\partial y} \left[\frac{\partial R}{\partial y}\right]^{-1} \frac{\partial R}{\partial x}$$

$$\psi$$

# Cost of adjoint evaluation is independent of the number of design variables





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### Wing aerodynamic shape optimization requires a high-fidelity model

Navier–Stokes equations

$$\frac{\partial w}{\partial t} + \frac{1}{A} \oint F_i \cdot \hat{n} dl - \frac{1}{A} \oint F_v \cdot \hat{n} dl = 0$$

$$w = \begin{bmatrix} \rho \\ \rho u_{1} \\ \rho u_{2} \\ \rho E \end{bmatrix} \quad F_{i_{1}} = \begin{bmatrix} \rho u_{1} \\ \rho u_{1}^{2} + p \\ \rho u_{1} u_{2} \\ (E + p) u_{1} \end{bmatrix} \quad F_{v_{1}} = \begin{bmatrix} 0 \\ \tau_{11} \\ \tau_{12} \\ u_{1}\tau_{11} + u_{2}\tau_{12} - q_{1} \end{bmatrix}$$
$$\tau_{11} = (\mu + \mu_{t}) \frac{M_{\infty}}{Re} \frac{2}{3} (2u_{1} - u_{2})$$
$$q_{1} = -\frac{M_{\infty}}{Re(\gamma - 1)} (\frac{\mu}{Pr} + \frac{\mu_{t}}{Pr_{t}}) \frac{\partial a^{2}}{\partial x_{1}}$$

[Shockwaves on wings]

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### Reynolds-averaged Navier–Stokes equations are solved in a 3D domain



Combine flow solver, adjoint solver, and gradient-based optimizer to enable design



#### Fast mesh deformation handles large design changes



Derivatives are obtained using the algorithmic differentiation adjoint (ADjoint)

Solve the governing equations

R(x,y(x))=0

form and solve the adjoint equations

$$\left[\frac{\partial R}{\partial y}\right]^T \psi = -\frac{\partial f}{\partial y}$$

and compute the derivatives

$$\frac{\mathrm{d}f}{\mathrm{d}x} = \frac{\partial f}{\partial x} + \psi^T \frac{\partial R}{\partial x}$$

[Mader et al., AIAA Journal, 2008]

### Common Research Model (CRM) wing is a new aerodynamic shape optimization benchmark



AIAA Aerodynamic Design Optimization Discussion Group (ADODG) Wing aerodynamic shape optimization requires hundreds of design variables



### Want to minimize drag by varying shape, subject to lift and geometric constraints

	Function/variable	Description	Quantity
minimize	$C_D$	Drag coefficient	
with respect to	$lpha _{z}$	Angle of attack FFD control point <i>z</i> -coordinates Total design variables	$egin{array}{c} 1 \\ 720 \\ 721 \end{array}$
subject to	$C_{L} = 0.5$ $C_{M_{y}} \ge -0.17$ $t \ge 0.25t_{\text{base}}$ $V \ge V_{\text{base}}$ $\Delta z_{\text{TE,upper}} = -\Delta z_{\text{TE,lower}}$ $\Delta z_{\text{LE,upper,root}} = -\Delta z_{\text{LE,lower,root}}$	Lift coefficient constraint Moment coefficient constraint Minimum thickness constraints Minimum volume constraint Fixed trailing edge constraints Fixed wing root incidence constraint Total constraints	$1 \\ 1 \\ 750 \\ 1 \\ 15 \\ 1 \\ 769$

### Started with a good design and made it 8.5% better [Lyu et al., AIAA Journal, 2014]



#### Now, let's start with a bad design!



#### Now, let's start with a really bad design!



#### The initial and optimized geometries and grids are available with the AIAA Journal paper as supplemental data



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Zhoujie Lyu, Gaetan K. W. Kenway, and Joaquim R. R. A. Martins. "Aerodynamic Shape Optimization Investigations of the Common Research Model Wing Benchmark"., doi: 10.2514/1.J053318

Current Issue Available Issues Articles in Advance

#### Aerodynamic Shape Optimization Investigations of the Common Research Model Wing Benchmark

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#### ABSTRACT

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Despite considerable research on aerodynamic shape optimization, there is no standard benchmark problem allowing researchers to compare results. This work addresses this issue by solving a series of aerodynamic shape optimization problems based on the Common Research Model wing benchmark case defined by the Aerodynamic Design Optimization Discussion Group. The aerodynamic model solves the Reynolds-averaged Navier-Stokes equations with a Spalart-Allmaras turbulence model. A gradient-based optimization algorithm

### 3D-printed models colored with $C_p$ distributions

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- Aerostructural design optimization
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# Wing design demands more than just aerodynamics



## Want to optimize both aerodynamic shape and structural sizing, with high-fidelity



### Sequential optimization is equivalent to coordinate descent



## Sequential optimization fails to find the multidisciplinary optimum



[Chittick and Martins, Struct. Multidiscip. O., 2008]

## MDO for Aircraft Configurations with High-fidelity (MACH)

#### Python user script

Setup up the problem: objective function, constraints, design variables, optimizer and solver options

Optimizer interface		Aerostructural solver		Geometry modeler
<i>pyOpt</i>		<i>AeroStruct</i>		<i>DVGeometry/GeoMACH</i>
Common interface to various		Coupled solution methods and coupled		Defines and manipulates
optimization software		derivative evaluation		geometry, evaluates derivatives
SQP	Other optimizers	Structural solver <i>TACS</i> Governing and adjoint equations	Flow solver <i>SUMad</i> Governing and adjoint equations	

- Underlying solvers are parallel and compiled
- Coupling done through memory only
- Emphasis on clean Python user interface
- Solver independent

[Kenway et al., AIAA J., 2014]

[Kennedy and Martins, Finite Elem. Des., 2014]

### Adjoint method efficiently computes gradients with respect to thousands of variables



[Kenway et al., AIAA J., 2014]

## A smooth function and accurate gradients keep the optimizer happy



#### Let's do aerostructural optimization!

![](_page_41_Figure_1.jpeg)

NASA-Michigan undeformed Common Research Model (uCRM)

## Optimize 973 "aerodynamic" and structural sizing design variables

![](_page_42_Figure_1.jpeg)

#### Objective and design variables

	Function/variable	Description	Quantity
minimize	$\beta$ Fuel burn + $(1 - \beta)$ TOGW		
with respect to	$x_{ m span}$	Wing span	1
	$x_{ m sweep}$	Wing sweep	1
	$x_{ m chord}$	Wing chord	1
	$x_{ m twist}$	Wing twist	8
	$x_{ m airfoil}$	FFD control points	192
	$x_{\mathrm{alpha}_i}$	Angle of attack at each flight condi-	12
	- •	tion	
	$x_{\eta_i}$	Tail rotation angle at each flight con-	12
		dition	
	$x_{\mathrm{throttle}_i}$	Throttle setting for each cruise flight	7
		condition	
	$x_{ m altitude}$	Cruise altitude	1
	$X_{ m CG}$	CG position	1
	$x_{ m skin \ pitch}$	Upper/lower stiffener pitch	2
	$x_{ m spar \ pitch}$	Le/Te Spar stiffener pitch	2
	$x_{ m ribs}$	Rib thickness	45
	$x_{ m panel\ thick}$	Panel thickness Skins/Spars	172
	$x_{ m stiff\ thick}$	Panel stiffener thickness Skins/Spars	172
	$x_{ m stiff\ height}$	Panel stiffener height Skins/Spars	172
	$x_{\rm panel\ length}$	Panel length Skin/Spars	172
		Total design variables	973

#### Constraints

subject to  $L = n_i W$  $C_{M_{y_i}} = 0.0$ T = D $1.08D - T_{\rm max} < 0$  $t_{\rm LE}/t_{
m LE_{Init}} \ge 1.0$  $t_{\mathrm{TE}}/t_{\mathrm{TE}_{\mathrm{Init}}} \geq 1.0$  $\mathcal{V}_{\mathrm{wing}} > \mathcal{V}_{\mathrm{fuel}}$  $x_{\rm CG} - 1/4MAC = 0$  $L_{\text{panel}} - x_{\text{panel length}} = 0$  $KS_{stress} \leq 1$  $KS_{buckling} \leq 1$  $\mathrm{KS}_{\mathrm{buckling}} \leq 1$  $KS_{buckling} \leq 1$  $KS_{buckling} \leq 1$  $\left| x_{\text{panel thick}_i} - x_{\text{panel thick}_{i+1}} \right| \le 0.0025$  $\left|x_{\text{stiff thick}_i} - x_{\text{stiff thick}_{i+1}}\right| \le 0.0025$  $x_{\mathrm{stiff \ height}_i} - x_{\mathrm{stiff \ height}_{i+1}}$  $x_{\text{stiff thick}} - x_{\text{panel thick}} < 0.005$  $\Delta z_{\mathrm{TE,upper}} = -\Delta z_{\mathrm{TE,lower}}$  $\Delta z_{\rm LE,upper} = -\Delta z_{\rm LE,lower}$ 

Lift constraint	12
Trim constraint	12
Thrust constraint	7
Excess thrust constraint	7
Leading edge radius	20
Trailing edge thickness	20
Minimum fuel volume	1
CG location at $1/4$ chord MAC	1
Target panel length	172
2.5 g Yield stress	4
2.5 g Buckling	3
-1.0 g Buckling	3
1.78 g Yield stress	3
1.78 g Buckling	4
Skin thickness adjacency	168
Stiffener thickness adjacency	168
Stiffener height adjacency	168
Maximum stiffener-skin difference	172
Fixed trailing edge	8
Fixed leading edge	8
Total constraints	<b>961</b>

## Considering multiple flight conditions is required for a practical design

- 7 cruise conditions for performance
- 2 off design conditions
- 3 maneuver condition for structural constraints
- Aircraft trimmed at all conditions

![](_page_45_Figure_5.jpeg)

![](_page_46_Figure_0.jpeg)

![](_page_47_Figure_0.jpeg)

### This framework enables designers to perform optimal objective and technology tradeoffs

![](_page_48_Figure_1.jpeg)

[Kennedy et al., AIAA 2014-0596]

# Boeing 777x will use folding wing tips to fit in current airport gates

![](_page_49_Picture_1.jpeg)

![](_page_49_Picture_2.jpeg)

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### Summary

- Efficient and accurate gradient computation via adjoints methods
- Robust aerodynamic shape optimization
- Extended adjoint method to multiple disciplines
- Aerostructural design optimization with respect to 1000 design variables
- Muito mais a fazer!

Currently using these tools to refine the next generation of aircraft

![](_page_52_Picture_1.jpeg)

Flexible high-aspect ratio wings [Kenway and Martins, AIAA 2015-2790]

![](_page_52_Picture_3.jpeg)

Truss-braced wing [Ivaldi, et al., AIAA 2015-3436]

![](_page_52_Picture_5.jpeg)

Blended-wing body [Lyu and Martins, *Journal of Aircraft*, 2014]

![](_page_52_Figure_7.jpeg)

Tow-steered composite [Brooks et al., 2015]

#### We are now extending the coupled-adjoint approach and developing a general framework for MDO

![](_page_53_Figure_1.jpeg)

![](_page_53_Picture_2.jpeg)

[Martins and Hwang, AIAA Journal, 2013]

### Vamos a optimizar!

John Hwang Peter Lyu Gaetan Kenway

**Graeme Kennedy** 

http://mdolab.engin.umich.edu/publications

![](_page_54_Picture_4.jpeg)

![](_page_54_Picture_5.jpeg)

### More information:

#### MDOIab Newsletter-Fall 2014

![](_page_55_Picture_2.jpeg)

#### Dear Friend,

Welcome to the MDOlab newsletter, an update on research and open source software that we send a few times a year. You are receiving this because I think you are interested in numerical optimization, MDO, engineering design, or aircraft design. If this is not the case, feel free to <u>unsubscribe</u>. If you know someone who might like to subscribe, please forward them this newsletter. Best regards, <u>Joacuim Martins</u>

![](_page_55_Figure_5.jpeg)

Latest publications

#### Wing aerodynamic shape optimization benchmark

![](_page_55_Picture_8.jpeg)

The AIAA <u>Aerodynamic Design Optimization Discussion</u> <u>Group</u> developed a series of benchmark cases. In this paper, we solve the RANS-based wing optimization problem, try to find multiple local minima, and solve a number of related wing design optimization problems. The initial and optimized geometries and meshes are <u>provided here</u>.

[Paper] [Preprint] [Optimization movie]

#### Aerodynamic design optimization of a blended-wing body aircraft

![](_page_55_Picture_12.jpeg)

This builds on our previous work on <u>stability-constrained flying</u> wing optimization. A series of RANS-based aerodynamic design optimization studies shows the tradeoffs between drag, trim, and stability for the NASA/Boeing BWB. The photo on the left shows <u>3D-printed models with pressure colormaps</u>.

[Paper] [Preprint]

#### Satellite multidisciplinary design optimization benchmark

![](_page_55_Picture_16.jpeg)

In collaboration with NASA and the <u>Michigan Exploration</u> Lab, we developed a new large-scale benchmark MDO problem, and solved a problem with 25,000 design variables and 2.2 million state variables by optimizing the data downloaded from a CubeSat subject to operational and physical constraints. This problem is now a <u>plugin</u> in the <u>OpenMDAO</u> open source project.

[Paper] [Preprint]

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#### http://mdolab.engin.umich.edu

![](_page_55_Picture_21.jpeg)

UNIVERSITY of MICHIGAN

### **Relevant publications**

- J. R. R. A. Martins and J. T. Hwang. Review and unification of methods for computing derivatives of multidisciplinary computational models. AIAA Journal, 51(11):2582–2599, November 2013. doi: 10.2514/1.J052184.
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- J. T. Hwang, D. Y. Lee, J. W. Cutler, and J. R. R. A. Martins. Large-scale multidisciplinary optimization of a small satellite's design and operation. Journal of Spacecraft and Rockets, 51(5):1648–1663, September 2014. doi: 10.2514/1.A32751.
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- 8. J. Y. Kao, J. T. Hwang, J. R. R. A. Martins, J. S. Gray, and K. T. Moore. A modular adjoint approach to aircraft mission analysis and optimization. In Proceedings of the AIAA Science and Technology Forum and Exposition (SciTech), Kissimmee, FL, January 2015. AIAA 2015-0136.